

# A High Rigidity Spectrometer for FRIB

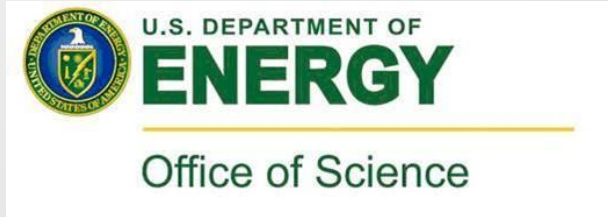
## Ion-optics Status Report

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HRS Working Group

Presented at the 2017 Low-Energy Community Meeting

[hrs.lbl.gov](https://hrs.lbl.gov)

ION-OPTICAL AND ASSOCIATED MAGNET FEASIBILITY  
STUDY FOR A HIGH RIGIDITY SPECTROMETER  
DOE Office of Science, Nuclear Physics DE-SC0014554



# Status ion-optical design of the HRS

## Outline

- HRS Spectrometer (this presentation) and [Beam Line \(Shumpei Noji\)](#)
- 5 Experiment types, design goals, design parameters and technical constraints
- Preferred ion-optical solution, 2 Modes (QQD, DQQ)
- Layout in planned building, ion-optics of 2 Modes
- Lattice files, disp. matching, magnet specifications
- Staging study
- Path forward for HRS

# How well does the preferred layout accomplish the design requirements?

## Optimize luminosity of experiments with fast rare-isotope beam at FRIB

|   |                                      |   |
|---|--------------------------------------|---|
| 1. Beam line and spectrometer that operate up to 8 Tm   | achieved                             | ✓ |
| 2. Transport beams of $\pm 15$ mrad (disp), $\pm 34$ mrad (non-disp), and $\pm 1.5\%$ ( $p$ ) to spectrometer | 100% transmission in achromatic mode | ✓ |

## Accommodate the Scientific program envision in the HRS white paper

|  |                                     |   |
|--|-------------------------------------|---|
| 3. In-beam $\gamma$ -ray spectroscopy  |                                     |   |
| a) at least 123 cm around target to place GRETA  | Exceeded (138 cm)                   | ✓ |
| b) $\pm 5\%$ acceptance ( $dE/E$ )   | Achieved                            | ✓ |
| 4. Invariant mass spectroscopy with neutrons   |                                     |   |
| a) $>90\%$ geometrical acceptance for neutrons emitted from 180 MeV/u $A=40$ nucleus for $E_x < 2$ MeV | Achieved                            | ✓ |
| b) neutron coverage in dispersive plane: $-6^\circ$ to $+20^\circ$                                     | Achieved                            | ✓ |
| c) Accommodate part of GRETA with only minor loss in neutron geometrical acceptance                    | 80% geometrical acceptance achieved | ✓ |
| d) $>10$ m flightpath to perform PID up to medium-mass nuclei (at least Sn region)                     | Exceeded (12.5 m)                   | ✓ |
| e) $\pm 10\%$ acceptance ( $dE/E$ )  | Achieved                            | ✓ |

# How well does the preferred layout accomplish the design requirements?

## Accommodate the Scientific program envision in the HRS white paper

|  |   |                              |
|--|---|------------------------------|
| <p>5. Knock-out experiments with beams up to <math>A \sim 200</math></p> <p>a) Dispersion-matched beam transport with optimized transmission through beam line</p> <p>b) PID up to mass 200 requires flightpath <math>&gt;25\text{m}</math> from HRS target to focal plane</p> <p>c) Resolving power <math>&gt; 1300</math> (momentum)</p>   | <p><math>\sim 50\%</math> achieved for <math>\pm 8\text{cm}</math> beamspot size</p> <p>Exceeded (<math>31.4\text{ m}</math>)</p> <p><math>\sim 10000</math> for <math>\pm 0.5\text{ mm}</math> beamspot size</p> | <p>✓</p> <p>✓</p> <p>✓</p>   |
| <p>6. Time-of-flight mass measurements</p> <p>a) Dispersion-matched beam transport with optimized transmission through beam line</p> <p>b) Mass resolution of better than 1 in 10000 requires <math>&gt;90\text{m}</math> flight path from fragment separator target to HRS focal plane</p> <p>c) Position resolution of <math>&lt;0.35\text{ mm}</math>; Time-of-flight resolution of <math>&lt;30\text{ ps}</math></p> | <p>Achieved</p> <p>Exceeded (<math>112\text{ m}</math>)</p> <p>Achievable – further detector development in progress</p>  | <p>✓</p> <p>✓</p> <p>...</p> |
| <p>7. In-flight fission experiments in which both fission fragments are measured in the focal plane of the HRS</p> <p>a) angular acceptances of <math>\pm 60\text{mrad}</math> in dispersive and non-dispersive plane</p> <p>b) PID up to mass 200 requires flightpath <math>&gt;25\text{m}</math> from HRS target to focal plane</p>  | <p>Exceeded:</p> <p><math>\pm 60\text{mrad}</math> (dispersive)</p> <p><math>\pm 90\text{mrad}</math> (nondisp.)</p> <p><math>31.4\text{ m}</math></p>  | <p>✓</p> <p>✓</p>            |

# Technical Considerations and Constraints

- Feasibility and Cost of large dipole and quadrupole magnets with Higher Order (HO) components (details see next slide)
- Realistic ion-optics that allows mechanical magnet design without interferences
- Space between magnets for detectors and diagnostic devices, GRETA needs 1.23 m along the beam, partial GRETA needs less space e.g. 0.9 m radius or smaller.
- Building constraints (design in progress)
  - North and South walls are existing
  - Shielding walls of about 2 m thickness
  - Clear passages of 96 inch around HRS
  - Beam line height is 1.25 m above floor, requires a 1.2 m pit below floor to accommodate large magnets

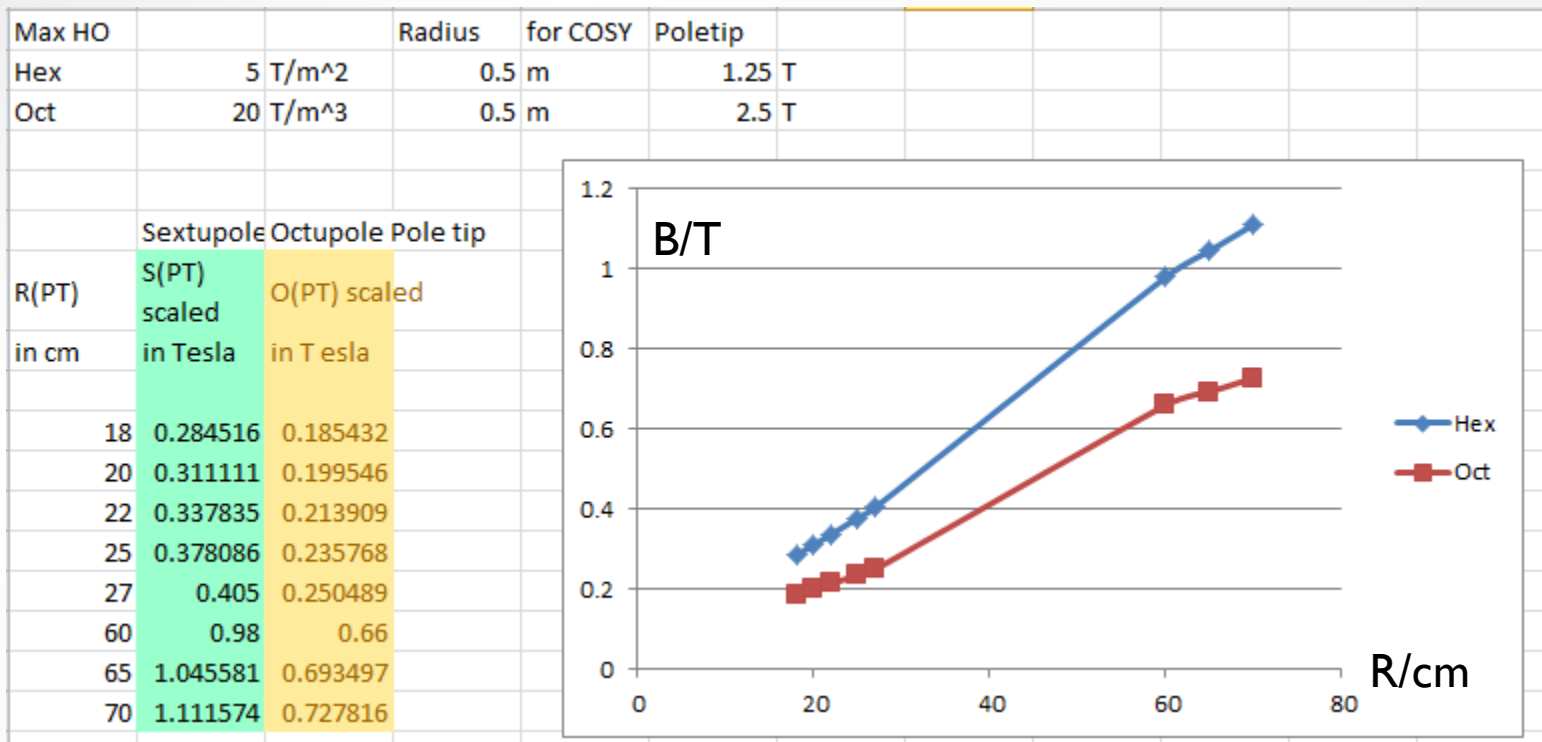
# Magnet design and Field Strength limits

- All magnet fields are iron dominated with superconducting coils
- Quadrupole magnets with Hex and Oct components Warm Bore radius is 10 cm smaller than the Cold Bore, warm bore determines maximum envelop

Dipole field strength maximum: Approx. 2.5 T

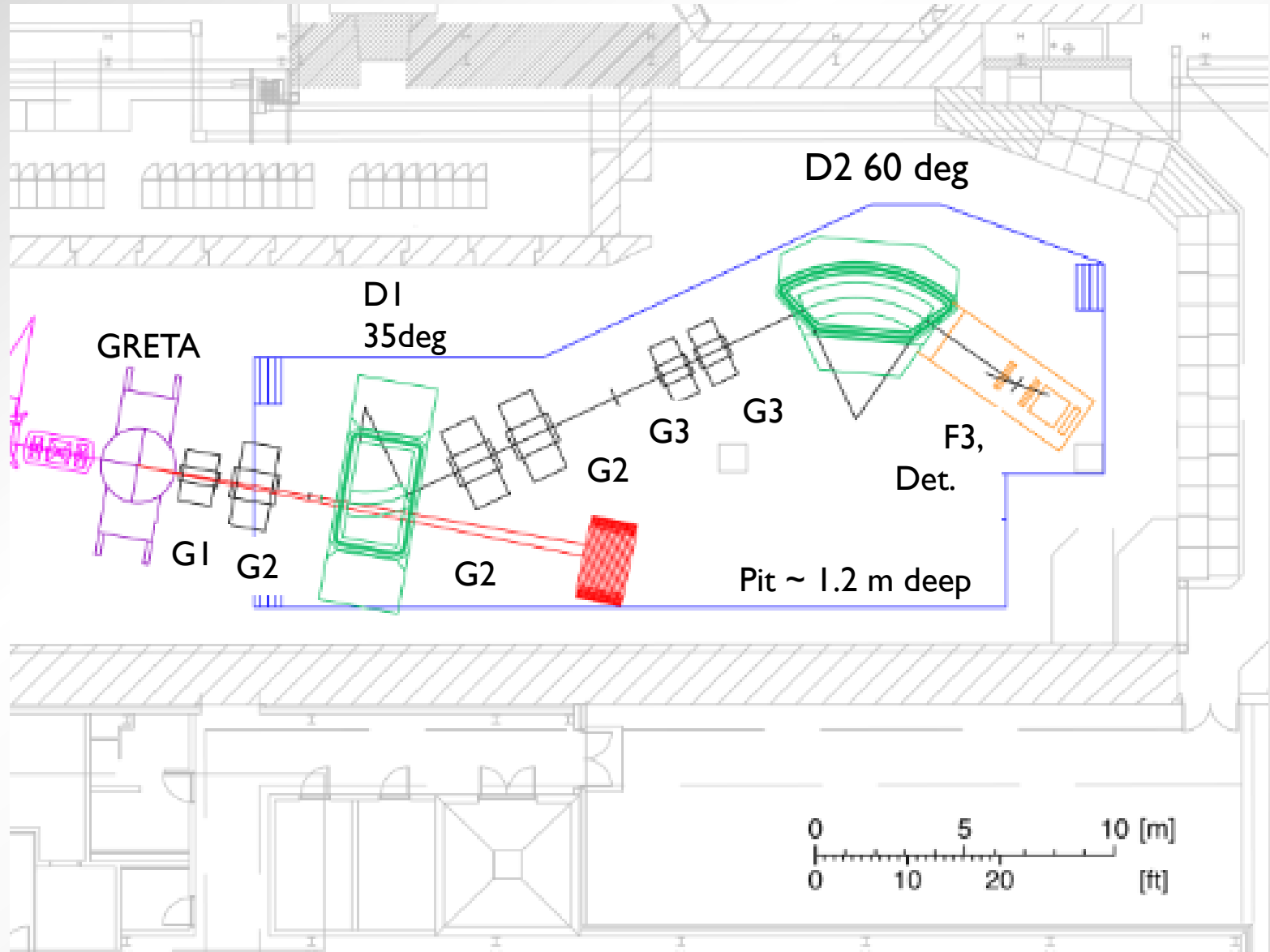
Quadrupole pole tip strength maximum at Cold Bore Radius: Approx. 2.5 T

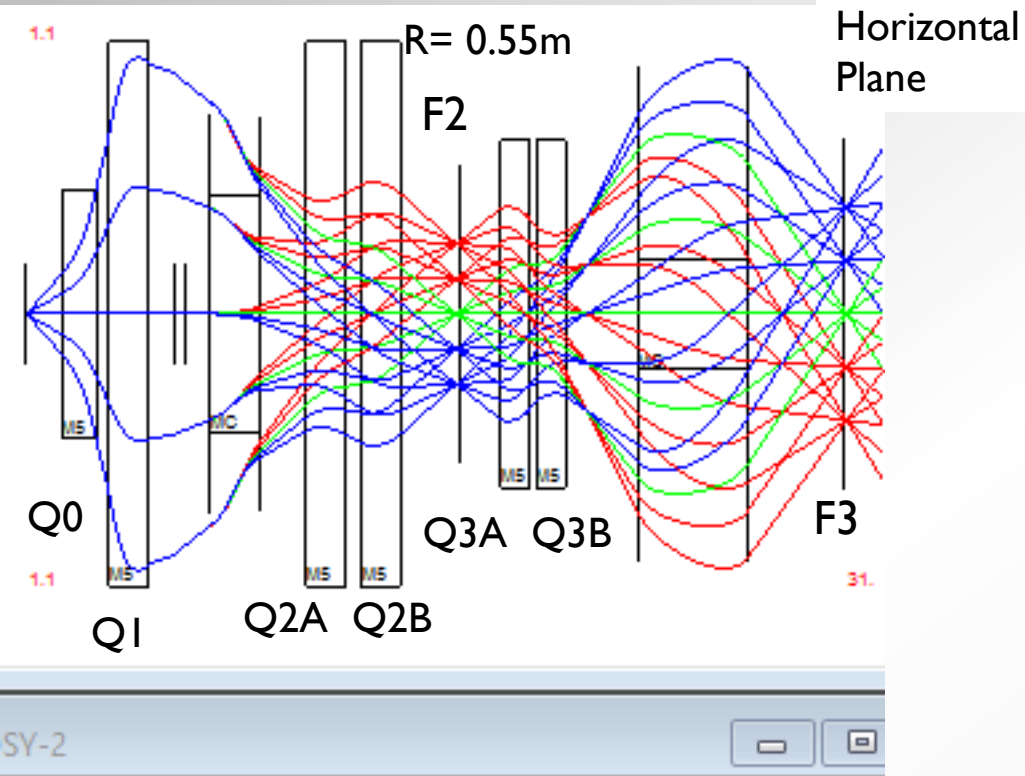
Max. HO pole tip strength B depends on the radius R (Ref. Shailendra Chouhan)



# Preferred Optics, Layout QQD Mode

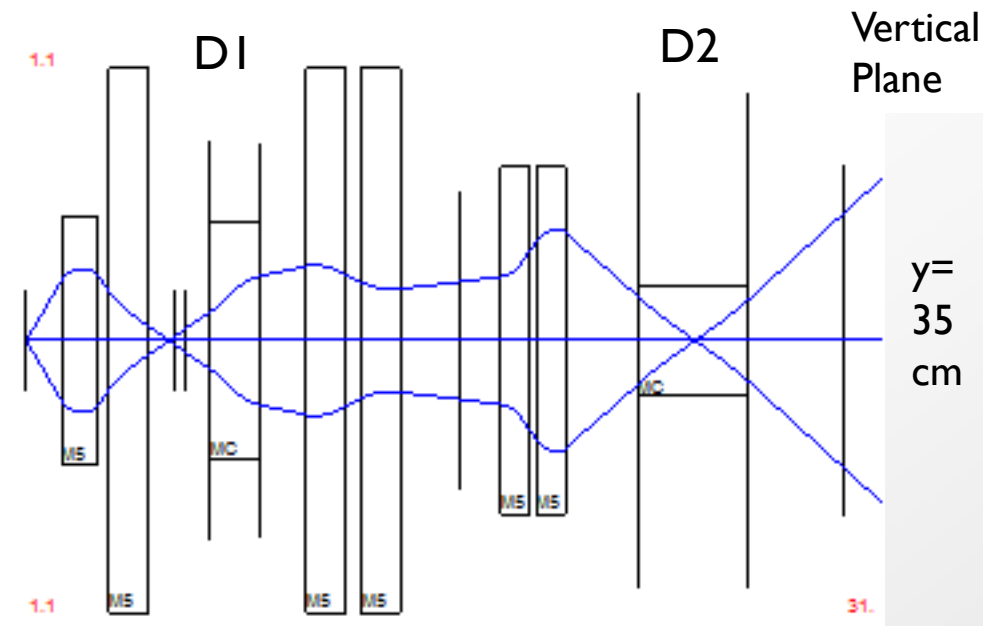
## Quadrupole Groups G1, G2, and G3





# QQD Preferred Optics, 1<sup>st</sup> order calc.

- Horiz. focus at F2 and F3
- Point-to-parallel from target to F2
- Vert. focus in D2 to minimize dipole gap





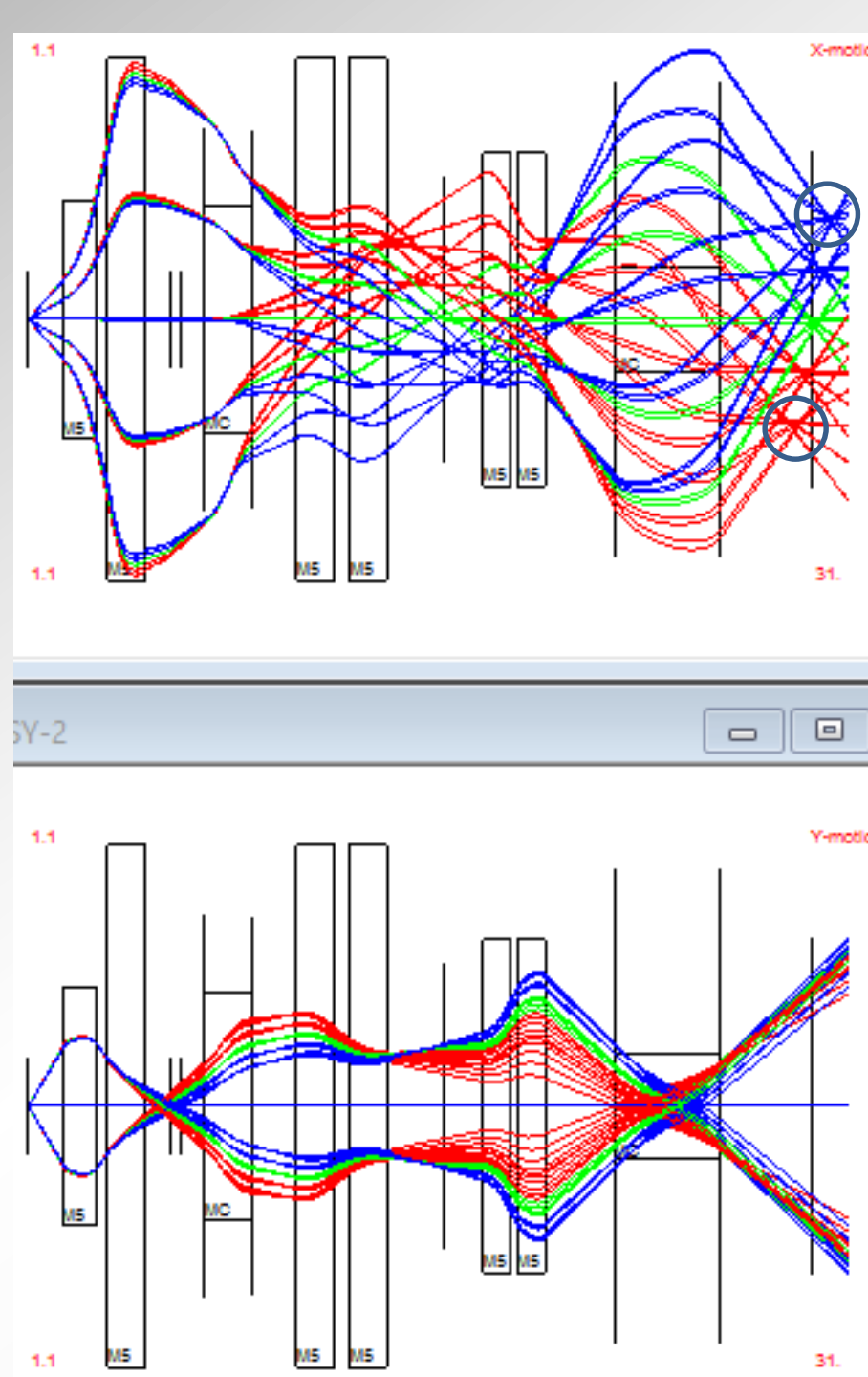
# QQD Preferred Optics, 2<sup>nd</sup> order calc.

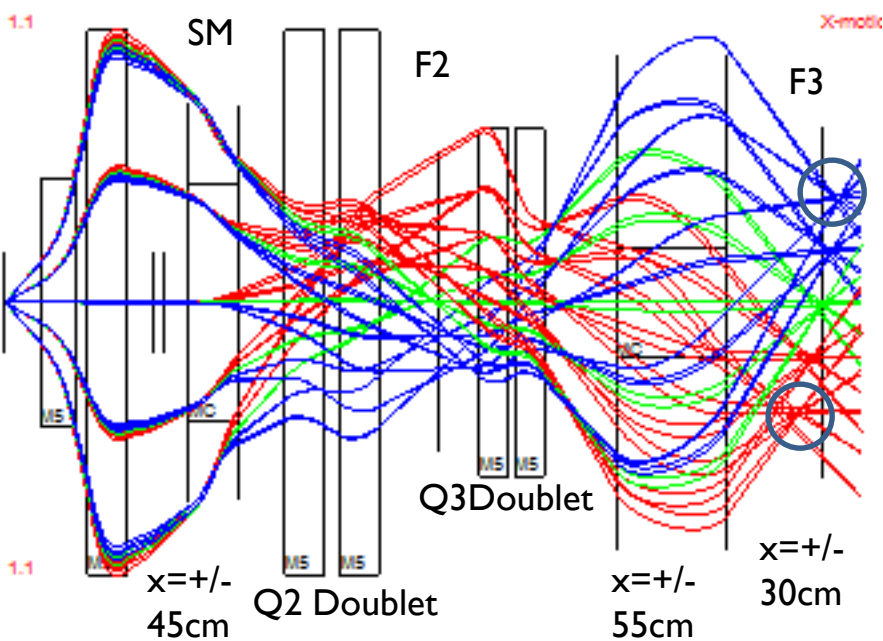
Focal Plane tilt angle: 74.0 deg

$$\text{Atan}(-\text{ME}(1,26)/\text{ME}(2,2)/\text{ME}(1,6))*180/\text{PI}$$

Notes:

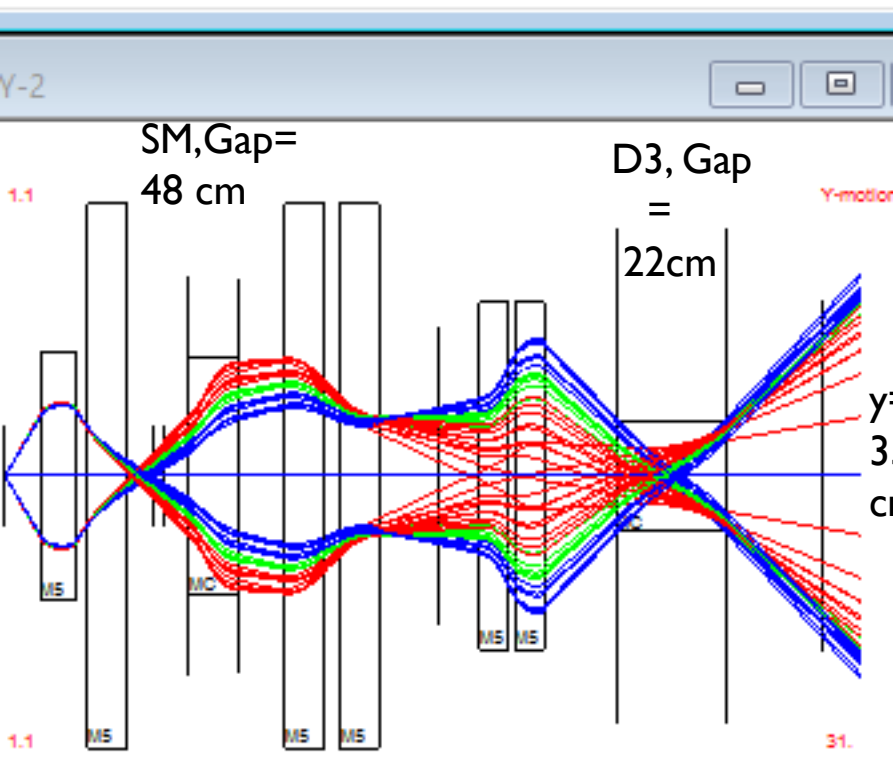
- Good focal points at F3
- In this drawing the warm bore R is shown, available for the particle envelop.





# Pref. Optics Optimized, QQD Mode, 7<sup>th</sup> order

Horizontal and vertical foci, F2/F3  
 DA =  $\pm 60$  mrad (Hor. Accept. Angle)  
 DB =  $\pm 90$  mrad (Vert. Accept. Angle)  
 dE/E =  $\pm 5\%$  (Energy Acceptance)  
 M11 = 1.343/-0.71158 (Hor. Magnif.)  
 M16 = 2.835/-4.2821 (Energy Disp.)  
 M21 = 0.217/-0.329  
 M26 = 0.08/-0.142 M33 = -1.11/4.41 Vert. Magn.  
 For  $x_0 = \pm 1\text{mm}$ , E-Res. Power(E) = -1055/3009  
 For  $x_0 = \pm 0.5\text{mm}$ , Res. Power d/dp  $\sim 12000$



|                  |             |               |
|------------------|-------------|---------------|
| Q0A := -2.4700;  | H0A := 0.0; | O0A := 0.21;  |
| Q1A := 2.1450;   | H1A := 0.0; | O1A := -0.10; |
| Q2A := -0.9800;  | H2A := 0.0; | O2A := 0.0;   |
| Q2B := 1.1500;   | H2B := 0.0; | O2B := 0.0;   |
| Q3A := 1.693194; | H3A := 0.0; | O3A := 0.0;   |
| Q3B := -2.01293; | H3B := 0.0; | O3B := 0.0;   |

Focal Plane tilt angle:  $-84.2/74.0$  deg  
 $\text{Atan}(-\text{ME}(1,26)/\text{ME}(2,2)/\text{ME}(1,6)) * 180/\text{PI}$

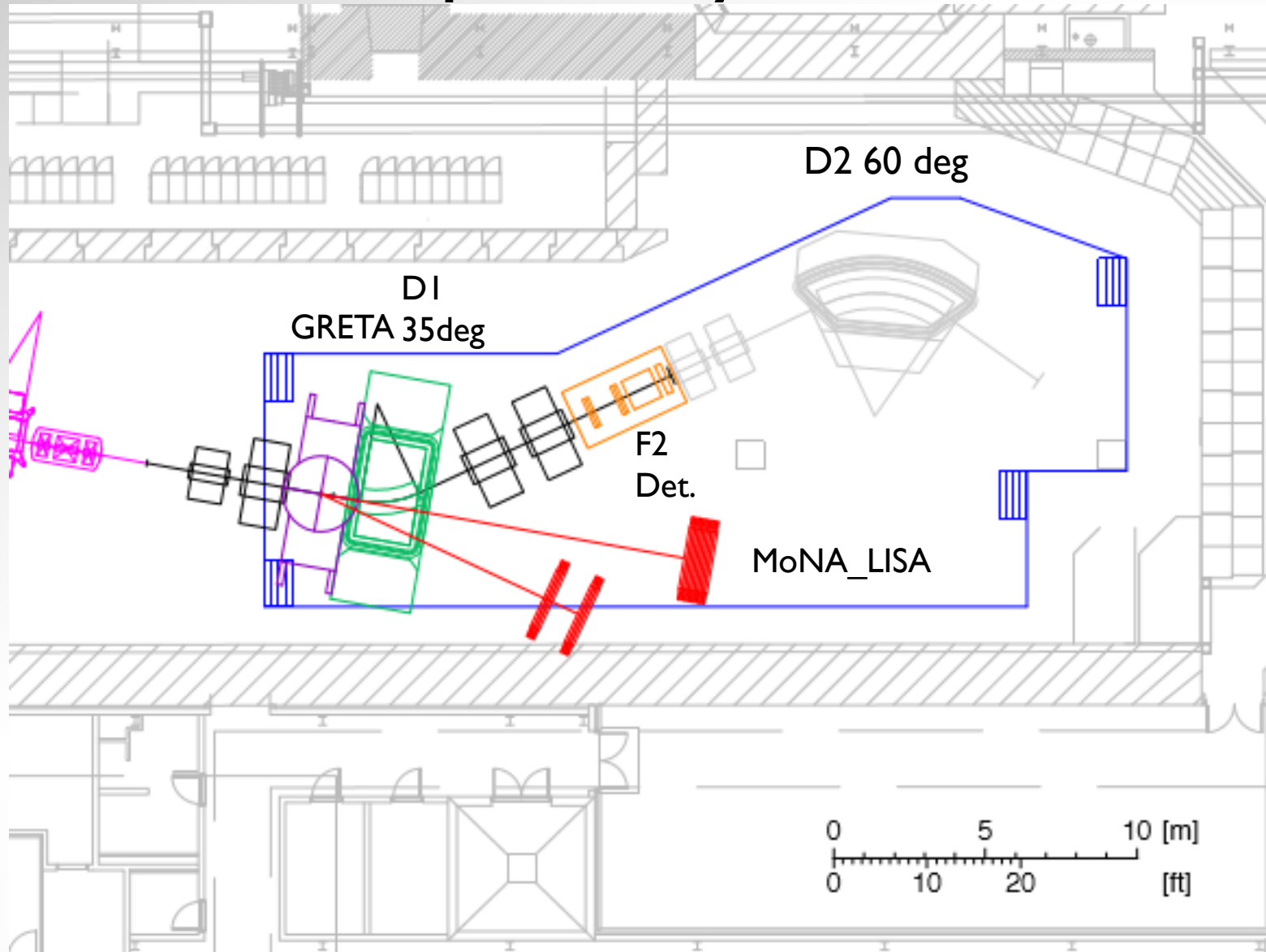
# Lattice File: Preferred Optics HRS, QQD Mode

| HRS Spectrometer layout         |             | 6/17/2017          | Preferred Optics, optimized |                             |               |           |          |      |        |           |
|---------------------------------|-------------|--------------------|-----------------------------|-----------------------------|---------------|-----------|----------|------|--------|-----------|
| HRS_Lattice_Pref_QQD_061717.xls |             | QQDQQQ mode        | File                        | HRS_QQD_12June_Q_length.fox |               |           |          |      |        | Cold bore |
| Element                         | Note        | Element properties |                             | Cold bore Radius/           | Warm bore (m) | Length(m) | Pole tip |      |        |           |
| Technical Name                  | Description | Effect. Length(m)  | Half gap (m)                | Dipole half gap             | Note          |           | Quad     | Hex  | Oct    |           |
|                                 |             | Dipole Bend Angle  |                             |                             |               |           |          |      |        |           |
|                                 |             |                    |                             |                             | FPI           |           |          |      |        |           |
| DL1                             | Drift       | 1.4                |                             |                             |               | 1.4       |          |      |        |           |
| Q0A                             | Quad+Oct    | 1.3                | 0.35                        | 0.25                        |               | 2.7       | -2.47    | 0.01 | 0.212  |           |
| DL2                             | Drift       | 0.45               |                             |                             |               | 3.15      |          |      |        |           |
| Q1A                             | Quad+Oct    | 1.5                | 0.65                        | 0.55                        |               | 4.65      | 2.145    | 0    | -0.094 |           |
| DL3                             | Drift       | 1.1                |                             |                             |               | 5.75      |          |      |        |           |
| DL4                             | Drift       | 0.4                |                             |                             |               | 6.15      |          |      |        |           |
| DL5                             | Drift       | 0.9                |                             |                             |               | 7.05      |          |      |        |           |
| D1/SM                           | Dipole      | 35                 | 3.2                         | 0.24                        | GFR=0.9m      | 9.0048    |          |      |        |           |
| DL6                             | Drift       | 1.75               |                             |                             |               | 10.75477  |          |      |        |           |
| Q2A                             | Quad        | 1.5                | 0.65                        | 0.55                        |               | 12.25477  | -0.98    | 0.1  | 0      |           |
| DL7                             | Drift       | 0.6                |                             |                             |               | 12.85477  |          |      |        |           |
| Q2B                             | Quad        | 1.5                | 0.65                        | 0.55                        |               | 14.35477  | 1.15     | 0.1  | 0      |           |
| DL8                             | Drift       | 2.25               |                             |                             | F2            | 16.60477  |          |      |        |           |
| DL9                             | Drift       | 1.6                |                             |                             |               | 18.20477  |          |      |        |           |
| Q3A                             | Quad        | 1.1                | 0.45                        | 0.35                        |               | 19.30477  | 1.693194 | 0    | 0      |           |
| DL10                            | Drift       | 0.3                |                             |                             |               | 19.60477  |          |      |        |           |
| Q3B                             | Quad        | 1.1                | 0.45                        | 0.35                        |               | 20.70477  | -2.01293 | 0.2  | 0      |           |
| DL11                            | Drift       | 2.8                |                             |                             |               | 23.50477  |          |      |        |           |
| D2                              | Dipole      | 60                 | 4                           | 0.11                        | GFR=1.1m      | 27.6936   |          |      |        |           |
| DL12                            | Drift       | 3.7                |                             |                             | FP3           | 31.39356  |          |      |        |           |

 HRS Length

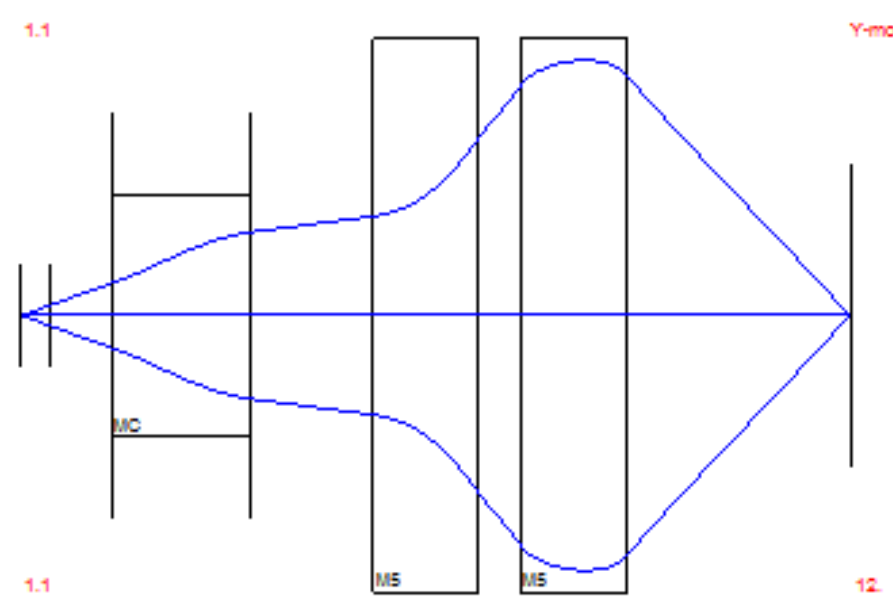
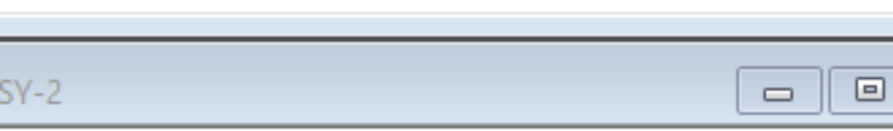
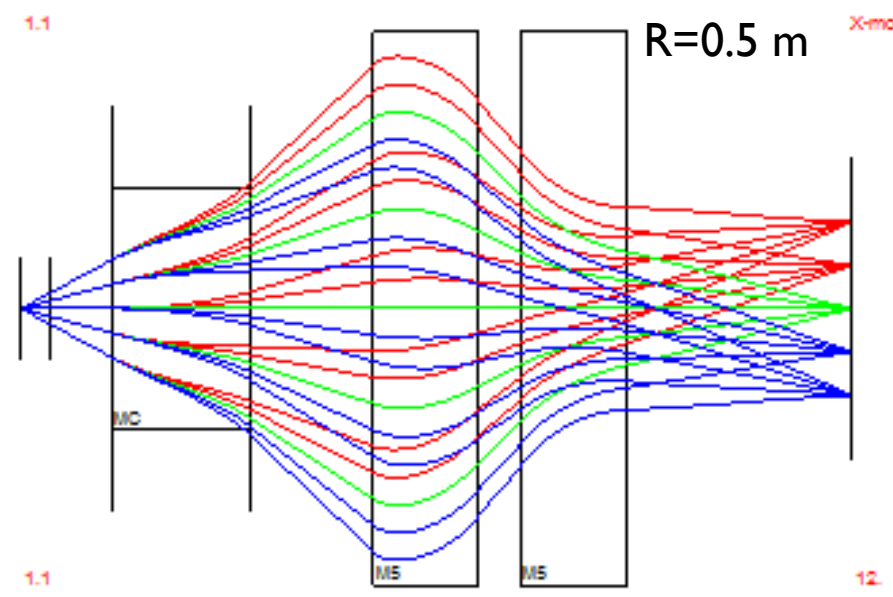
Design Note: All quadrupoles are assumed to have Hexapole and Octupole components, so the Cold Bore Radius is 0.1 m larger than the Worm Bore Radius.  
 Although not all quads used all HO coils, it is assumed that in the further optimization the radial HO components in the dipoles and quads will require such components.  
 Also all types of quads (Q0A, Q1A = Q2A = Q2B, Q3A = Q3B) are kept identical .

# Preferred Optics, Layout DQQ Mode



Full GRETA is shown. In this mode only partial GRETA (Distance 1.3 m to DI one detector ring removed, 0.9 m two detector rings removed) will be used.

Preferred DQQ mode,  
1<sup>st</sup> order calc.

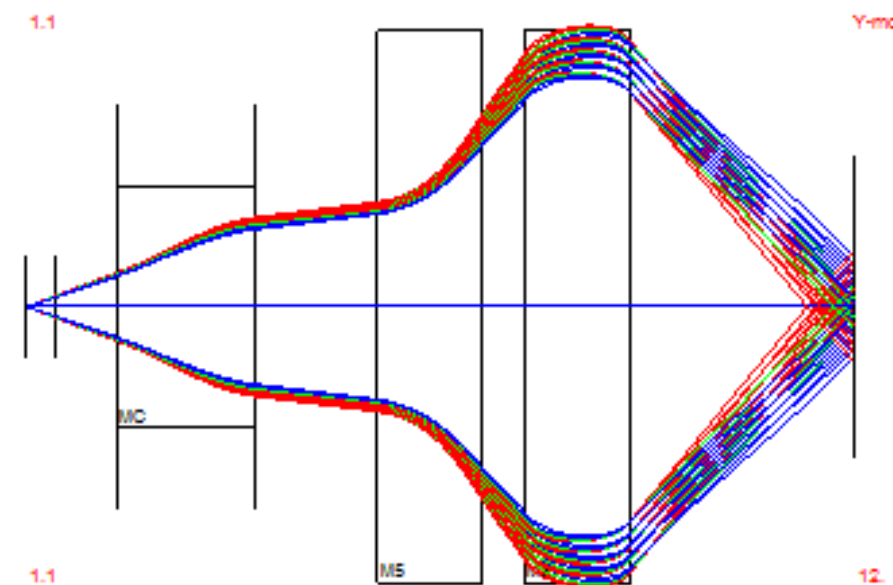
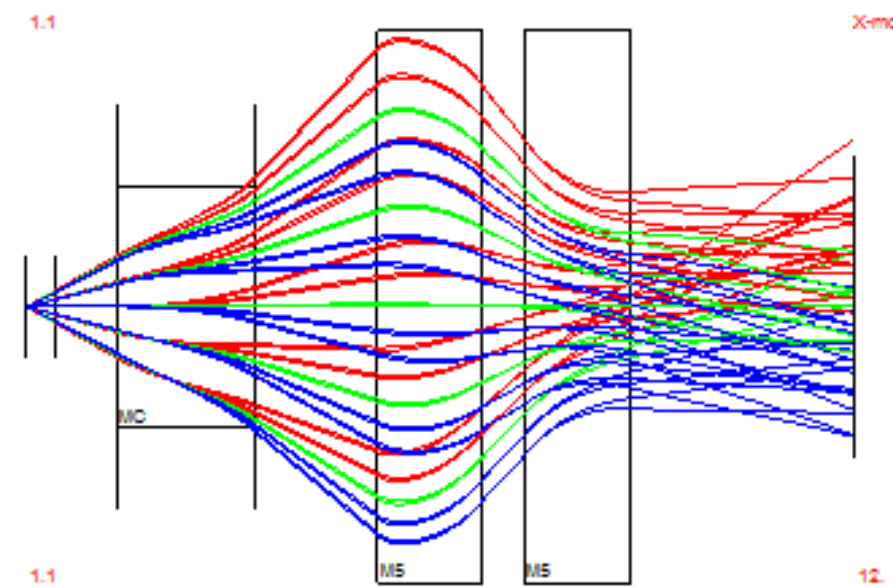


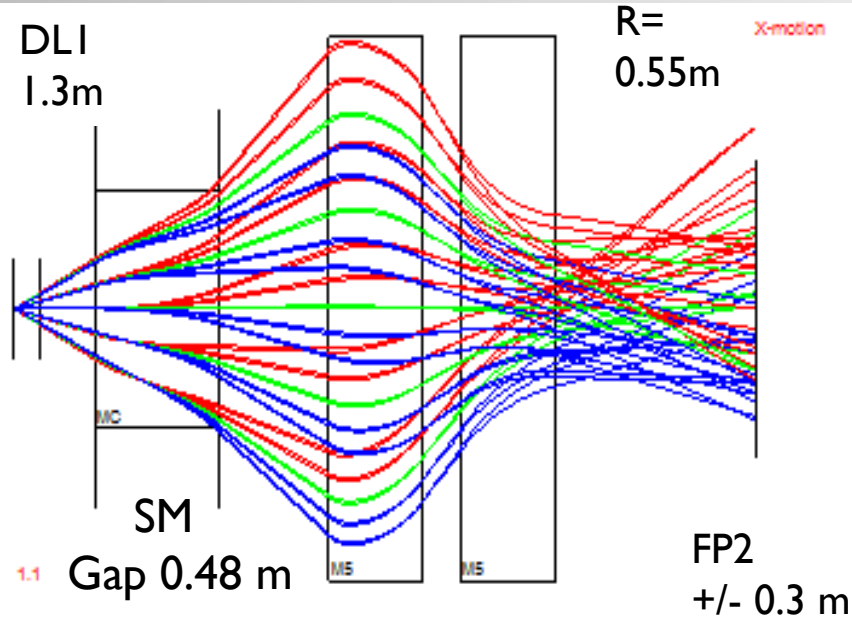
# Preferred DQQ mode, 2<sup>nd</sup> order calc.

Note:

In this drawing the warm bore R is shown, that is available for the particle envelop .

If no HO components are needed the  
Cold Bore = Warm Bore





## Preferred DQQ Mode, 4<sup>th</sup> order DLI = 1.3 m

Horizontal and vertical foci, F2

DA = 75 mrad (Hor. Accept. Angle)

DB = 50 mrad (Vert. Accept. Angle)

dE/E = 10% (Energy Acceptance)

M11 = 2.222 (Hor. Magnif.)

M16 = 1.721 (Energy Disp.)

M21 = 0.552

M26 = 0.277

For  $x_0 = \pm 1$  mm, E-Resolv. Power 387

$x_0 = 0.5$  mm, p-Resol. Power  $p/dp \sim 1500$

M33 = -0.329

Cold Bore 0.65m

Q2A:= 2.420;

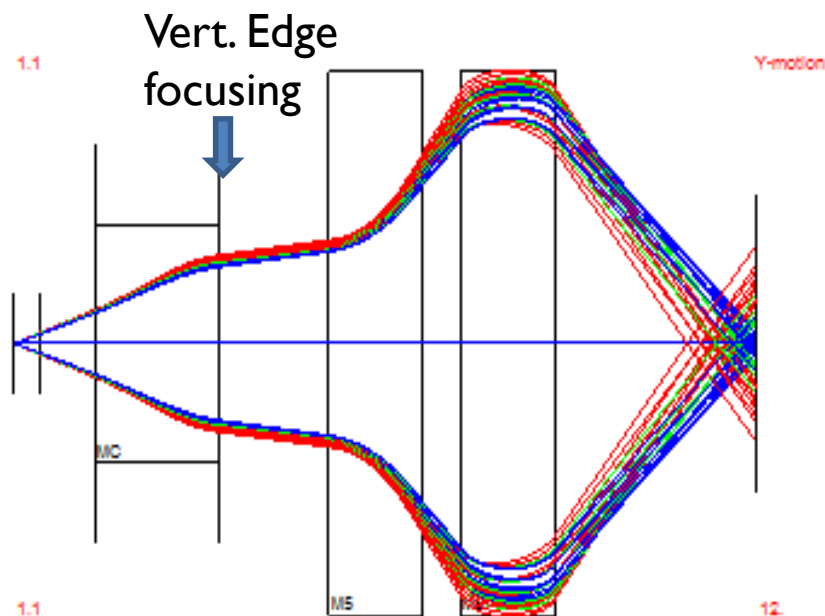
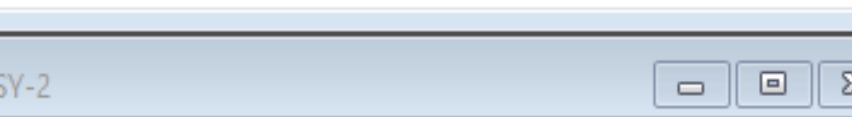
H2A= 0.1

O2A :=0;

Q2B:= -2.560

H2B= 0.1

O2B :=0;



**File: HRS\_DQQ\_12June\_Q\_length.fox**



# Lattice File: Preferred Optics HRS, DQQ Mode

|                                  |             |                    |      |                             |                 |          |           |          |     |     |  |  |
|----------------------------------|-------------|--------------------|------|-----------------------------|-----------------|----------|-----------|----------|-----|-----|--|--|
| HRS_Lattice_Pref_DQQ_062117.xlsx |             | DQQ mode           | File | HRS_DQQ_12June_Q_length.fox |                 |          |           |          |     |     |  |  |
| Element                          | Note        | Element properties |      | Cold bore Radius/           | Warm bore (m)   |          | Length(m) | Pole tip |     |     |  |  |
| Technical Name                   | Description | Effect. Length(m)  |      | Half gap (m)                | Dipole half gap | Note     |           | Quad     | Hex | Oct |  |  |
|                                  |             | Dipole Bend Angle  |      |                             |                 |          |           |          |     |     |  |  |
|                                  |             |                    |      |                             |                 | FPI      |           |          |     |     |  |  |
| DL4                              | Drift       | 0.4                |      |                             |                 |          | 0.4       |          |     |     |  |  |
| DL5                              | Drift       | 0.9                |      |                             |                 |          | 1.3       |          |     |     |  |  |
| D1/SM                            | Dipole      | 35                 |      | 3.2                         | 0.24            | GFR=0.5m | 3.2548    |          |     |     |  |  |
| DL6                              | Drift       | 1.75               |      |                             |                 |          | 5.004769  |          |     |     |  |  |
| Q2A                              | Quad        | 1.5                |      | 0.65                        | 0.55            |          | 6.504769  | 2.42     | 0.1 | 0   |  |  |
| DL7                              | Drift       | 0.6                |      |                             |                 |          | 7.104769  |          |     |     |  |  |
| Q2B                              | Quad        | 1.5                |      | 0.65                        | 0.55            |          | 8.604769  | -2.56    | 0.1 | 0   |  |  |
| DL8                              | Drift       | 3.2                |      |                             |                 | F2       | 11.80477  |          |     |     |  |  |
| DL9                              | Drift       | 0.65               |      |                             |                 | shifted! | 12.45477  |          |     |     |  |  |

Design Notes: Focal Plane F2 have different locations for the QQD and DQQ modes. GFR for D1 in QQD mode is 0.9 m but only 0.5 m in DQQ mode.

Polarities of Q2A and Q2B are reversed for QQD and DQQ mode. Bipolar power supplies or switches are needed.



# Dispersion Matching Preferred Optics

following solutions are obtained [12] for the beam-line parameters  $b_{16}$  and  $b_{26}$  to realize lateral dispersion matching and angular dispersion matching, respectively.

$$b_{16} = -\frac{s_{16}}{s_{11}}(1 + s_{11}s_{26}K - s_{21}s_{16}K)\frac{C}{T} \quad (7)$$

and

$$b_{26} = (s_{21}s_{16} - s_{11}s_{26})C. \quad (8)$$

See e.g. H. Fujita, NIM A484 (2002) 17

$b$  = beam line 1<sup>st</sup> order matrix elements

$s$  = spectrometer 1<sup>st</sup> order matrix elements

Assumptions:

$K = 0$  at 0 deg Scatt.Angle

$T = 1$  at 0 deg and perpend.Target

$C = (p_{in}/p_{out})/(dp_{out}/dp_{in})$

$C = 1$  for elastic scattering

Matching conditions:

$$b_{16} = -s_{16}/s_{11}$$

$$b_{26} = s_{21}s_{16} - s_{11}s_{26}$$

| HRS Preferred, update 7/24/2017 |             |                              |        |       |        |        |       | Test Rays |        |        |
|---------------------------------|-------------|------------------------------|--------|-------|--------|--------|-------|-----------|--------|--------|
| COSY: *. fox file               |             | HRS_dispersion_Matching.xlsx |        |       |        | [m]    | [rad] | DE =      |        |        |
|                                 | Focal Plane | s11                          | s16    | s21   | s26    | b16    | b26   |           | x/m    | DA/rad |
| HRS_QQD_12June_Q_length.fox     | F2          | 1.343                        | 2.835  | 0.217 | 0.08   | -2.111 | 0.508 | 0.010     | -0.021 | 0.005  |
| HRS_QQD_12June_Q_length.fox     | F3          | -0.712                       | -4.282 | -0.33 | -0.142 | -6.018 | 1.308 | 0.040     | -0.241 | 0.052  |
| HRS_DQQ_130_Pref_12May_2017.fox | F2          | 2.222                        | 1.721  | 0.552 | 0.277  | -0.775 | 0.334 | 0.100     | -0.077 | 0.033  |
| HRS_Staging_D_40deg.fox         | F3          | -0.981                       | -4.81  | -0.34 | 0.0344 | -4.903 | 1.669 | 0.100     | -0.490 | 0.167  |

# Dipole Specifications, HRS Preferred Optics

|                           | Units       | D1     | D2     |
|---------------------------|-------------|--------|--------|
| Bending radius            | m           | 3.2    | 4      |
| Max. rigidity             | Tm          | 8      | 8      |
| Max. magn. field          | Tm          | 2.5    | 2      |
| Bending angle, + to right | deg         | -35    | 60     |
| Central ray arc           | m           | 1.9548 | 4.1888 |
| Vert. gap, full size      | m           | 0.48   | 0.22   |
| GFR, dB/B < +/- 0.5%      | m           | 0.9    | 1.1    |
| Pole width, approx.       | m           | 2.34   | 1.6    |
| Edge angle, entrance      | deg         | 0      | -20    |
| Edge angle, exit          | deg         | 35     | -20    |
| Total height, approx.     | m           | 4.8    | 2.8    |
| Weight, approx.           | metric tons | 650    | 400    |

# Quadrupole Specifications

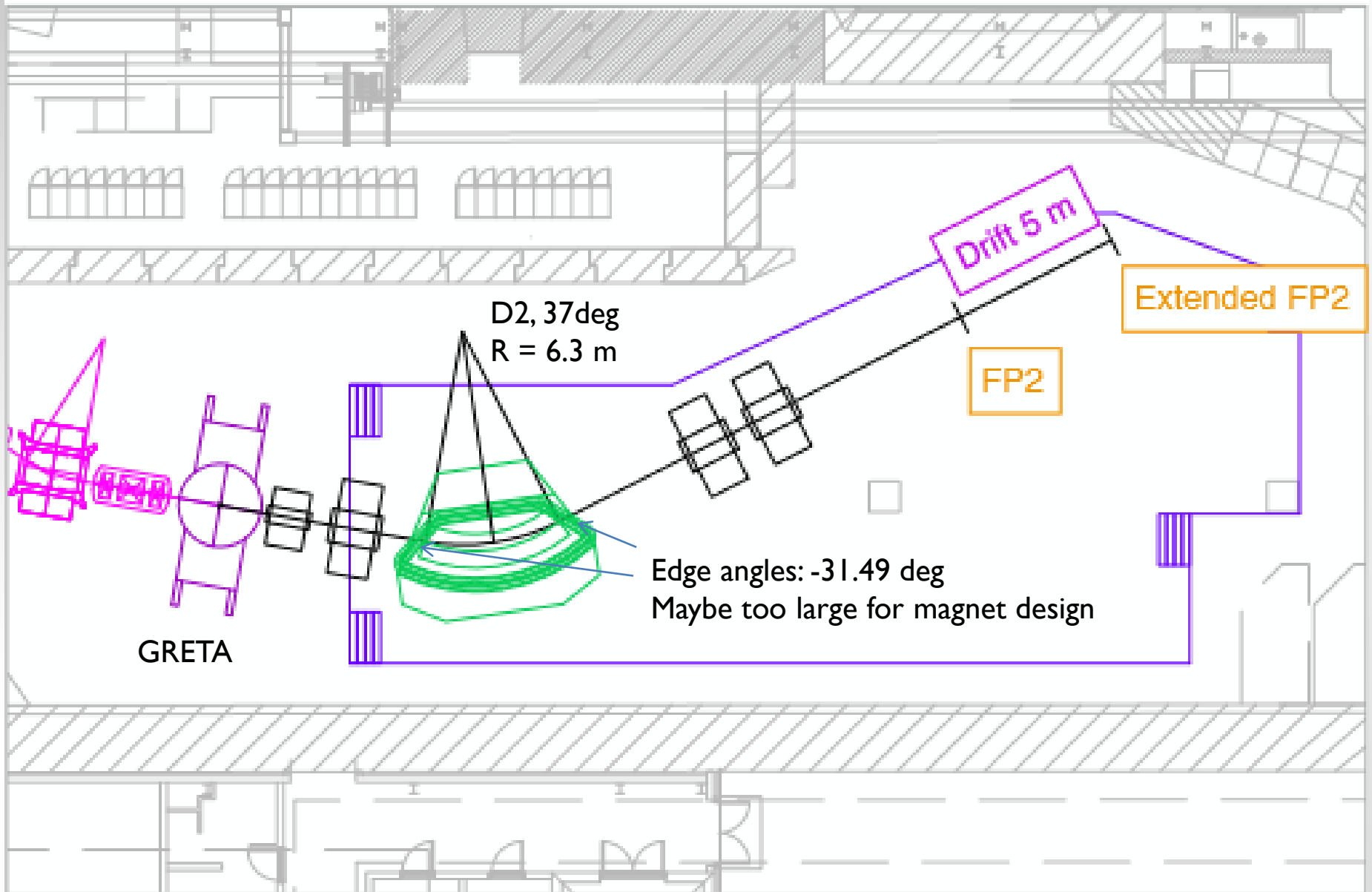
## HRS Preferred Optics (QQD Mode)

|                        | Units | Q0A   | Q1A  | Q2A   | Q2B  | Q3A  | Q3B   |
|------------------------|-------|-------|------|-------|------|------|-------|
| Focusing strength      | T     | -9.64 | 5.31 | -2.71 | 2.71 | 4.28 | -5.14 |
| Eff. Field length      | m     | 1.25  | 1.25 | 1.25  | 1.25 | 1.1  | 1.1   |
| Max. gradient          | T/m   | -7.71 | 4.25 | -2.17 | 2.17 | 3.89 | -4.67 |
| Cold bore, radius      | m     | 0.35  | 0.6  | 0.6   | 0.6  | 0.45 | 0.45  |
| Warm bore, radius      | m     | 0.25  | 0.5  | 0.5   | 0.5  | 0.45 | 0.45  |
| Max. pole tip strength | T     | -2.7  | 2.55 | -1.3  | 1.3  | 1.75 | -2.1  |
| Max. inhomogeneity     | %     | 0.2   | 0.2  | 0.2   | 0.2  | 0.2  | 0.2   |

# Staging

- Staging study to stretch the HRS project in time to avoid spikes in funds and manpower.
- Consider impact on science program.
- All large magnets of Stage 1 have to be used in Stage 2, to make staging affordable.
- Stage 2 has to fulfill all of the spectrometer requirements.
- We studied several concepts, the present Staging Option is the most promising.
- Consider impact on science program for shutdown, additional cost for staging, like vacuum chambers, longer management, risk

# Staging Layout (QQD Mode)



## Stage Optics, 3<sup>rd</sup> Order

Horizontal and vertical foci, **F3**

DA = +/- 40 mrad (Hor. Accept. Angle)

DB = +/- 90 mrad (Vert. Accept. Angle)

dE/E = +/- 5% (Energy Acceptance)

M11 = -0.981 (Hor. Magnif.)

M16 = -4.810 (Energy Disp.)

M21 = -0.340

M26 = 0.0344 M33 = 3.851 Vert. Magn.

For  $x_0 = +/- 1$  mm, E-Res. Power(E) = 245 l

For  $x_0 = +/- 0.5$  mm, Res. Power d/dp ~ 9600

Q0A := -1.824;

H0A := 0.0;

O0A := 0.0;

Q1A := 0.521;

H1A := 0.0;

O1A := 0.0;

Q2A := -1.856;

H2A := 0.0;

O2A := 0.0;

Q2B := 1.110;

H2B := 0.0;

O2B := 0.0;

H3A := 0.0;

O3A := 0.0;

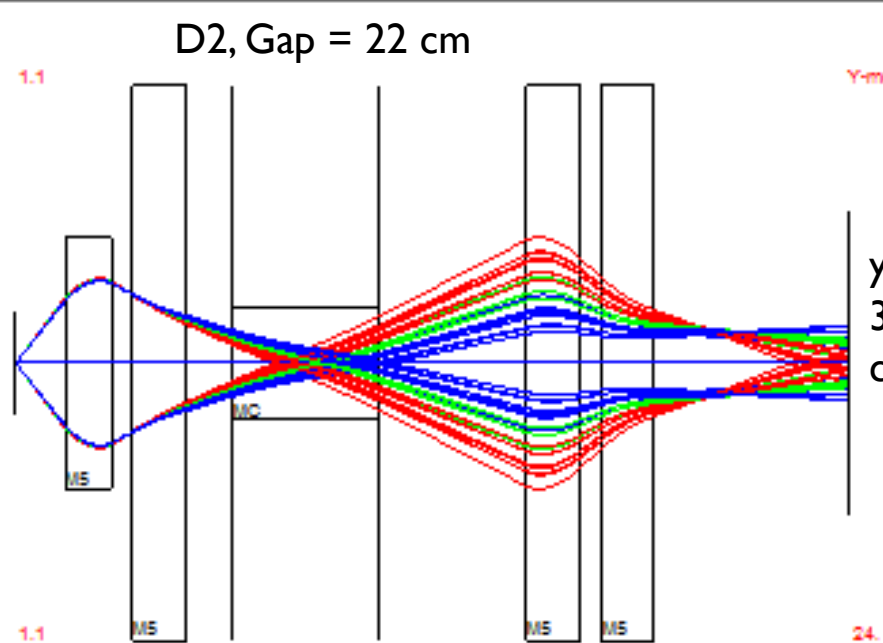
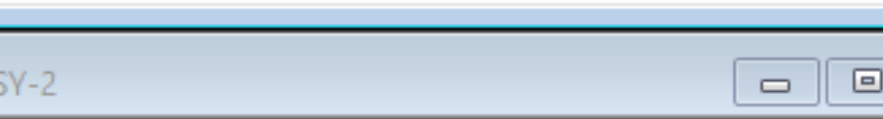
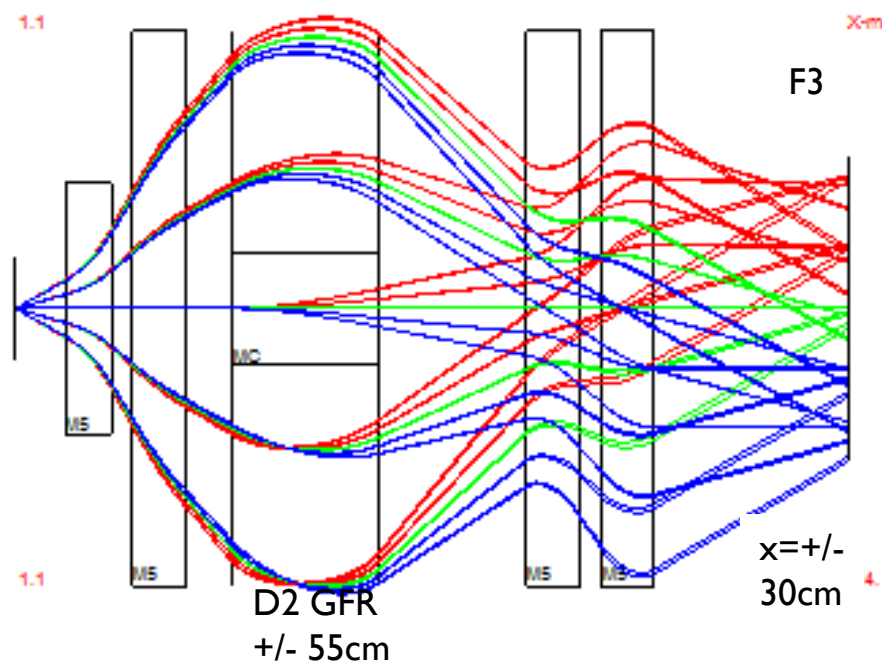
H3B := 0.0;

O3B := 0.0;

Focal Plane tilt angle: -79.0 deg

$\text{Atan}(-\text{ME}(1,26)/\text{ME}(2,2)/\text{ME}(1,6)) * 180/\text{PI}$

File: HRS\_Staging\_D\_40deg.fox



# Lattice File: Staging Optics HRS (QQD Mode)

| HRS Spectrometer layout         |             | 7/24/2017          | Stage D        |                         |               |           |          |     |                    |
|---------------------------------|-------------|--------------------|----------------|-------------------------|---------------|-----------|----------|-----|--------------------|
| HRS_Lattice_Stage_D_072417.xlsx |             | QQD Mode           | File           | HRS_Staging_D_40deg.fox |               |           |          |     | Cold bore Pole tip |
| Element                         | Note        | Element properties |                | Cold bore Radius/       | Warm bore (m) | Length(m) | T        |     |                    |
| Technical Name                  | Description | Effect. Length(m)  | Bending radius | Dipole half gap         | Note          |           | Quad     | Hex | Oct                |
|                                 |             | Dipole Bend Angle  |                |                         | FPI           |           |          |     |                    |
| DL1                             | Drift       | 1.4                |                |                         |               | 1.4       |          |     |                    |
| Q0A                             | Quad+Oct    | 1.3                | 0.35           | 0.25                    |               | 2.7       | -1.824   | 0   | 0                  |
| DL2                             | Drift       | 0.6                |                |                         |               | 3.3       |          |     |                    |
| Q1A                             | Quad+Oct    | 1.5                | 0.65           | 0.55                    |               | 4.8       | 0.520999 | 0   | 0                  |
| DL3                             | Drift       | 1.35               |                |                         |               | 6.15      |          |     |                    |
| DL4                             | Drift       | 0                  |                |                         |               | 6.15      |          |     |                    |
| DL5                             | Drift       | 0                  |                |                         |               | 6.15      |          |     |                    |
| D2                              | Dipole      | 37.02              | 6.3            | 0.11                    | GFR=1.1m      | 10.2206   |          |     |                    |
| DL6                             | Drift       | 4.2                |                |                         |               | 14.42056  |          |     |                    |
| Q2A                             | Quad        | 1.5                | 0.65           | 0.55                    |               | 15.92056  | -1.8561  | 0   | 0                  |
| DL7                             | Drift       | 0.6                |                |                         |               | 16.52056  |          |     |                    |
| Q2B                             | Quad        | 1.5                | 0.65           | 0.55                    |               | 18.02056  | 1.11     | 0   | 0                  |
| DL8                             | Drift       | 5.5                |                |                         | F3            | 23.52056  |          |     |                    |

Design Notes: All quadrupoles and dipole D2 in this stage are identical (same specifications) as those with the same name in the full HRS system, magnet settings are different.

In this Stage , there is no Sweeper magnet (D1) and also Q3A and Q3B are not presents.

In this Stage dipole D2 is used with different bending radius and edge angles.

In this Stage several drift lengths are different from the full HRS system, requiring new vacuum chambers in the transition from Stage to full HRS system.

All quadrupoles are assumed to have Hexapole and Octupole components, so the Cold Bore Radius is 0.1 m larger than the Warm Bore Radius.

Although not all quads used all HO coils, it is assumed that in the further optimization the radial HO components in the dipoles and quads will require such components.

Also all types of quads (Q0A, Q1A = Q2A = Q2B) are identical .

# Path forward for HRS

- Field calculations of magnets to minimize size of large magnets, extract HO (inside, ends, and fringe fields), perform ion-optical calculations, iterate if necessary.
- Specify Hexapole and Octupoles built into quadrupoles.
- Tolerances, calculate and specify.



**END**